

# Maxwell's Equations

In terms of the  $\mathbf{E}$  and  $\mathbf{B}$  fields Maxwell's equations are

## Maxwell's Equations

$$\nabla \cdot \mathbf{E} = \frac{\rho}{\epsilon_0}$$

$$\nabla \cdot \mathbf{B} = 0$$

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}$$

$$\nabla \times \mathbf{B} = \mu_0 \mathbf{J} + \mu_0 \epsilon_0 \frac{\partial \mathbf{E}}{\partial t}.$$

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In terms of the electromagnetic field strength tensor  $F^{\mu\nu}$  Maxwell's equations can be encapsulated by the single equation

## Maxwell's Equations

$$\partial_\mu F^{\mu\nu} = j^\nu$$

where  $F^{\mu\nu} = \partial^\mu A^\nu - \partial^\nu A^\mu$  and  $A^\mu = (\Phi, \mathbf{A})$  is the EM 4-potential, and  $j^\nu = (\rho, \mathbf{J})$  is the EM 4-current.