## MATH 54 - QUIZ 2

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Name: $\qquad$
Instructions: You have 15 minutes to take this quiz, for a total of 10 points. May your luck be linearly independent!

1. (4 points) Determine for which $c$ the following vectors are linearly independent:

$$
\left[\begin{array}{c}
3 \\
-6 \\
1
\end{array}\right],\left[\begin{array}{c}
-6 \\
4 \\
-3
\end{array}\right],\left[\begin{array}{l}
9 \\
c \\
3
\end{array}\right]
$$

2. (6 points total) Suppose $T: \mathbb{R}^{3} \longrightarrow \mathbb{R}^{2}$ is a linear transformation such that:

$$
T\left[\begin{array}{l}
1 \\
0 \\
0
\end{array}\right]=\left[\begin{array}{l}
2 \\
4
\end{array}\right] \quad T\left[\begin{array}{l}
0 \\
1 \\
0
\end{array}\right]=\left[\begin{array}{l}
3 \\
6
\end{array}\right] \quad T\left[\begin{array}{c}
2 \\
-1 \\
2
\end{array}\right]=\left[\begin{array}{l}
1+4 c \\
2+2 c
\end{array}\right]
$$

(a) (4 points) Find the matrix of $T$
(b) (1 point) For which $c$ is $T$ one-to-one? Justify briefly
(c) (1 point) For which $c$ is $T$ onto $\mathbb{R}^{2}$ ? Justify briefly

